

Simulation Based on Michel Fodje's epr-simple simulation translated from Python to Mathematica by John Reed 13 Nov 2013 also with Quaternions Modified by Fred Diether for Joy's S³ Quaternion Completely Local-Realistic Model Nov. 2021

Load Quaternion Package, Set Run Time Parameters, Initialize Arrays and Tables

```
In[429]:= << Quaternions`
β0 = Quaternion[1, 0, 0, 0];
β1 = Quaternion[0, 1, 0, 0];
β2 = Quaternion[0, 0, 1, 0];
β3 = Quaternion[0, 0, 0, 1];
Qcoordinates = {β1, β2, β3};
m = 20000;
trialDeg = 721;
Ls1 = ConstantArray[0, m];
Ls2 = ConstantArray[0, m];
λ1 = ConstantArray[0, m];
λ2 = ConstantArray[0, m];
outA = Table[{0, 0}, m];
outB = Table[{0, 0}, m];
plotq = Table[{0, 0}, m];
Da1 = ConstantArray[0, m];
Db1 = ConstantArray[0, m];
a1 = ConstantArray[0, m];
b1 = ConstantArray[0, m];
A = ConstantArray[0, m];
B = ConstantArray[0, m];
φ = 3; β = 0.3; ξ = - $\frac{\pi}{12}$ ; (*Adjustable parameters for fine tuning*)
```

Generating Particle Data with Three Independent Do-Loops

```
In[451]:= Do[e = RandomReal[{-179, 180}]; (*Singlet vector angle*) (*Hidden Variable*)
λ1[[i]] = β (Cos[ $\frac{e}{\phi}$ ]^2);
λ2[[i]] = Sign[e];
ee = N[Flatten[{FromPolarCoordinates[{1, e * π/180}], 0}]];
Ls1[[i]] = λ2[[i]] * ee.Qcoordinates;
Ls2[[i]] = -λ2[[i]] * ee.Qcoordinates, {i, m}]

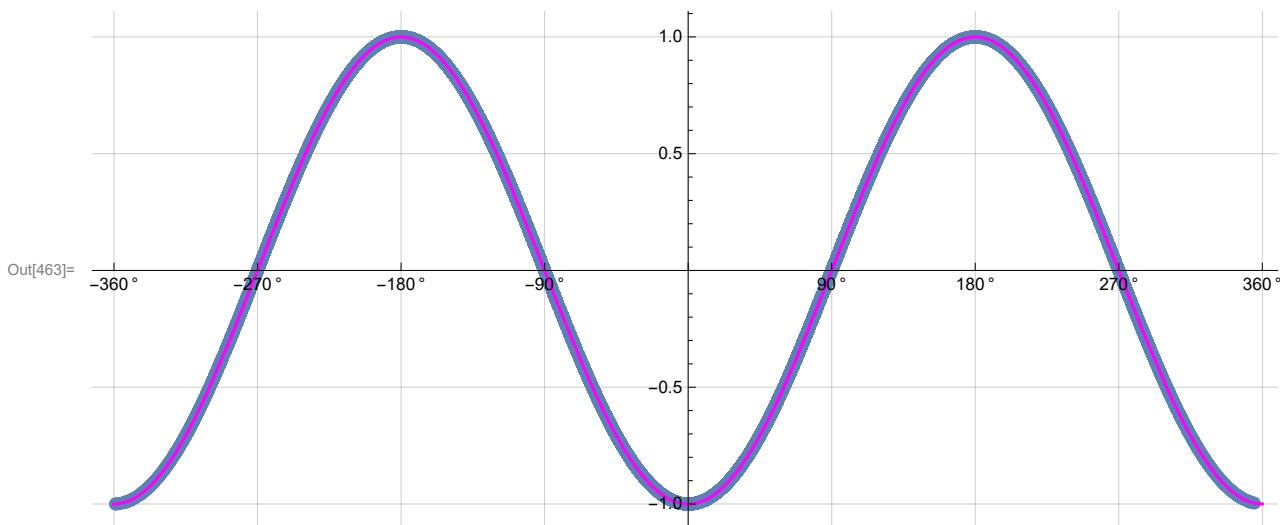
In[452]:= Do[a = RandomInteger[{-179, 180}]; (*Detector vector angle 1 degree increments*)
aa = N[Flatten[{FromPolarCoordinates[{1, a * π/180}], 0}]];
Da = aa.Qcoordinates; (*Convert to quaternion coordinates*)
Da1[[i]] = Da;
qa = Da ** Ls1[[i]];
If[Abs[Re[qa]] > λ1[[i]],
A = Re[Da ** Limit[Ls1[[i]], Ls1[[i]] -> Sign[Re[Da ** Ls1[[i]]]] Da]],
A = λ2[[i]] * Sign[qa[[4]] + ξ]];
outA[[i]] = {a, A}, {i, m}]
```

```
In[453]:= Do[b = RandomInteger[{-179, 180}]; (*Detector vector angle 1 degree increments*)
  bb = N[Flatten[{FromPolarCoordinates[{1, b *  $\pi$ /180}], 0}]];
  Db = bb.Qcoordinates; (*Convert to quaternion coordinates*)
  Db1[[i]] = Db;
  qb = Ls2[[i]] ** Db;
  If[Abs[Re[qb]] >  $\lambda$ 1[[i]],
    B = Re[Db ** Limit[Ls2[[i]], Ls2[[i]] -> Sign[Re[Db ** Ls2[[i]]]]] Db],
    B = - $\lambda$ 2[[i]] * Sign[qb[[4]] +  $\xi$ ]];
  outB[[i]] = {b, B}, {i, m}]
```

Product Calculation

```
In[454]:= a1 = outA[All, 1]; b1 = outB[All, 1]; A = outA[All, 2]; B = outB[All, 2];
q = 0; s = 0; t = 0; u = 0;
Do[If[ $\lambda$ 2[[i]] == 1,
  q = Limit[{Da1[[i]] ** Ls1[[i]] ** Ls2[[i]] ** Db1[[i]]}, {Ls1[[i]], Ls2[[i]]} ->
    {Sign[Re[Da1[[i]] ** Ls1[[i]]]] Da1[[i]], Sign[Re[Db1[[i]] ** Ls2[[i]]]] Db1[[i]]}],
  q = Limit[{Db1[[i]] ** Ls2[[i]] ** Ls1[[i]] ** Da1[[i]]}, {Ls1[[i]], Ls2[[i]]} ->
    {Sign[Re[Da1[[i]] ** Ls1[[i]]]] Da1[[i]], Sign[Re[Db1[[i]] ** Ls2[[i]]]] Db1[[i]]}]];
angle = a1[[i]] - b1[[i]];
s = s + q; t = t + A[[i]]; u = u + B[[i]];
plotq[[i]] = {angle, Re[q]}, {i, m}]
Meanq = FromQuaternion[s / m]; (*shows vanishing of the non-real part iK*)
Print["Meanq = ", Meanq]
aveA = t / m;
aveB = u / m;
Print[" <A> = ", aveA, " <B> = ", aveB]
simulation1 = ListPlot[plotq, PlotMarkers -> {Automatic, Small}, AspectRatio -> 7 / 16,
  Ticks -> {{{-360, -360  $^\circ$ }, {-270, -270  $^\circ$ }, {-180, -180  $^\circ$ }, {-90, -90  $^\circ$ }, {0, 0  $^\circ$ }, {90, 90  $^\circ$ },
    {180, 180  $^\circ$ }, {270, 270  $^\circ$ }, {360, 360  $^\circ$ }}, Automatic}, GridLines -> Automatic];
negcos1 = Plot[-Cos[x Degree], {x, -360, 360}, PlotStyle -> {Magenta}];
Show[simulation1, negcos1]

Meanq = (-0.00164109 + 0. i) + 0.00168218 K
<A> = -0.0036 <B> = -0.0021
```



Blue is the correlation data and magenta is the -cosine curve for an exact match.